Computer Graphics - WebGL2* (Questions)

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What is the Mandelbrot set, how is it defined?

• The Mandelbrot set is the set of complex numbers c, for which

$$f_c(z) = z^2 + c$$

does not diverge, when we iterate with the sequence

$$f_c(0), f(f(0)), f(f(f(c))), \dots$$

Let z = 0.5 + 0.5i, is this complex number in the Mandelbrot set?

$$f_c(z) = z^2 + c$$

 $z \cdot z = (a^2 - b^2) + (2ab)i$

Let z = 0.5 + 0.5i, is this point in the Mandelbrot set?

$$f_c(0) = 0^2 + \frac{1}{2} + \frac{1}{2}i = \frac{1}{2} + \frac{1}{2}i$$

$$f_c(\frac{1}{2} + \frac{1}{2}i) = (\frac{1}{2^2} - \frac{1}{2^2}) + (2 \cdot \frac{1}{2} \cdot \frac{1}{2})i + \frac{1}{2} + \frac{1}{2}i = \frac{1}{2} + 1i$$

$$f_c(\frac{1}{2} + 1i) = (\frac{1}{2^2} - 1^2) + (2 \cdot \frac{1}{2} \cdot 1)i + \frac{1}{2} + \frac{1}{2}i = -\frac{1}{4} + \frac{3}{2}i$$

$$f_c(-\frac{1}{4} + \frac{3}{2}i) = (\frac{1}{4^2} - \frac{3^2}{2^2}) + (2 \cdot \frac{-1}{4} \cdot \frac{3}{2})i + \frac{1}{2} + \frac{1}{2}i = -\frac{27}{16} - \frac{1}{4}i$$

 $|f_c^n(0)| \le 2$ for all n

Possible Questions

• Let's check:

$$f_c^4(0) = 3.2852 + 1.3438i$$

 $|f_c^4(0)| \approx \sqrt{3.2852^2 + 1.3438^2} \approx 3.5494$

• Length exceeds 2 so it is not in the Mandelbrot set